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# Machine Learning for Structural Classification and Monitoring (2<sup>nd</sup> Year) ELIA FAVARELLI

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### Last year...: Proposed strategy



### Last year: Results and problems

### **Results:**

- 4 Accuracy = 95%
- $\bigstar \text{ Missed detection} = 5\%$
- False alarm = 5%

### Main Problems:

- It is often impossible to have training data of weak conditions in real scenarios
- It is impossible to train Convolutional Neural Networks with only one class
- Comparison with literature





### Timeline



- Stochastic subspace identification (SSI)
- Principal component analysis (PCA)
- Kernel PCA (KPCA)
- Gaussian mixture model (GMM)
- Autoassociative neural network (ANN)

- **characteristics**
- Temperature effects
- Damage condition
- Database management
- ✤ Accelerometer data
- \*\* Environment data
- \*\* **Down sampling**
- \*\* **Decimation**
- \*\* Filtering

Machine learning

algorithms for

topology inference

Sensor failure effects

Quantization effects

Sensor failure

detection

### Z-24 bridge: structure description



- Classical posttensioned concrete two-cell box girder bridge with a main span of 30m and two side spans of 14m
- Long term monitoring in standard condition for 1 year
- Short term monitoring in progressive damage condition
- 15 accelerometers equipped
- 9 failures during the monitoring period
- 8 reliable sensors used for the following processing

### Z-24 bridge: Monitoring phases

4 August	Undamaged condition
9 August	Installation of pier settlement system
10 August	Lowering of pier, 20 mm
12 August	Lowering of pier, 40 mm
17 August	Lowering of pier, 80 mm
18 August	Lowering of pier, 95 mm
19 August	Lifting of pier, tilt of foundation
20 August	New reference condition
25 August	Spalling of concrete at soffit, 12 m <sup>2</sup>
26 August	Spalling of concrete at soffit, 24 m <sup>2</sup>
27 August	Landslide of 1 m at abutment
31 August	Failure of concrete hinge
2 September	Failure of 2 anchor heads
3 September	Failure of 4 anchor heads
7 September	Rupture of 2 out of 16 tendons
8 September	Rupture of 4 out of 16 tendons
9 September	Rupture of 6 out of 16 tendons

Nomenclature

- f<sub>s</sub> = sample frequency [Hz]
- $T_a = acquisition time [s]$
- $N_s =$  number of samples
- $N_{a} =$  number of acquisitions

### LONG TERM MONITORING

- For 1 year each hour an acquisition is taken from all the sensors:
  - $f_s = 100 \text{ Hz}$

$$T_{a} = 655.36 \text{ s}$$

•  $N_s = 65536$ 

### SHORT TERM MONITORING

On the left the progressive damage generated artificially by a lowering system

\* Unfortunately around 44% of the data have been lost

•  $N_{\alpha} = 4107$ 

### Finite element method

Pros:

• Accurate estimation of modal parameters

Cons:

- Computationally complex
- Need an accurate knowledge of the structure
- Not generalizable

### **Peak Picking**

Pros:

- Low complexity
- Blind method

Cons:

- Low accuracy in the modal parameter estimation
- Input sensitive

### ARMA method

Pros:

- No need of accurate knowledge of the structure
- Generalizable

### Cons:

- Computationally **complex**
- Convergence problems

### OMA: Output-only models



•  $H_{s}(\omega) = narrowband$ 

### Result

•  $F(\omega)$  excite all the modes of  $H_s(\omega)$ 

### OMA: Stochastic subspace identification (SSI)



### SSI method

Pros:

- No need of an accurate knowledge about the structure
- No need of a structure simulation (blind method)
- Output-only model
- Closed form solution
- Good accuracy in the modal parameter estimation
   Cons:
- Computationally complex

- i = time lag
- I = number of sensors

### Modal parameters (output)

- f = Natural frequencies (scalar)
- $\Lambda = \text{Eigenvalues (vector)}$
- $\Delta =$  Dumping ratios (scalar)
- $\Phi = Mode shapes (matrix)$

\*parameters extracted for each measurement (each hour)

### **OMA: Stabilization diagram**



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### Mode selection techniques: MAC

$$MAC(\mathbf{\Phi}^{(j)}, \mathbf{\Phi}^{(l)}) = \frac{|\mathbf{\Phi}^{(j)*}\mathbf{\Phi}^{(l)}|}{||\mathbf{\Phi}^{(j)}||_2^2 ||\mathbf{\Phi}^{(l)}||_2^2}$$

- Dimensionless correlation coefficient between mode shapes
- Takes value between 0 and 1, values larger than 0.9 indicate consistent correspondence and probably physical modes

### Mode selection techniques: MPD



- Indicator of the mode shape components deviation with respect to the mean phase (MP)
- Singular value decomposition (SVD):  $\mathbf{USV}^T = [\operatorname{Re}\{\Phi^{(j)}\} \operatorname{Im}\{\Phi^{(j)}\}]$
- $\mathbf{U} \in \mathbb{R}^{2 \times 2}$ ,  $\mathbf{S} \in \mathbb{R}^{2 \times 2}$  and  $\mathbf{V} \in \mathbb{R}^{2 \times 2}$

$$MP(\Phi_{j}) = \arctan\left(\frac{-V_{12}}{V_{22}}\right)$$
$$MPD(\Phi_{j}) = \frac{\sum_{k=1}^{n_{y}} |\Phi_{jk}| \arccos\left|\frac{\operatorname{Re}\{\Phi_{jk}\}V_{22} - \operatorname{Im}\{\Phi_{jk}\}V_{12}}{\sqrt{V_{12}^{2} + V_{22}^{2}}|\Phi_{jk}|}\right|}{\sum_{k=1}^{n_{y}} \Phi_{jk}}$$

• When  $\frac{MPD(\Phi_j)}{90^\circ} < 0.75$  the mode is considered spurious

- Dumping ratios check: for each mode we have a dumping ratio δ(j), in real structures this factor must be positive and lower than 0.2 (otherwise the structure will be unstable) hence only modes with 0<δ(j)<0.2 are considered</li>
- Complex conjugate poles check: if the eigenvalues of a mode do not have a complex conjugate probably represent a spurious mode and will be deleted, moreover if Re{λ(j)}>0 the mode represent an unstable structure hence the relative mode will be considered as spurious

### Cleaning & Clustering



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### Tracking: Algorithm

### Starting phase:

- 200 h of measurements
- Rectangular window, size=0.2 Hz, without overlap, range [0, 10Hz]
- Select the more relevant componets as starting points

### Online phase:

- n = iteration number
- 3 h of measurements
- Gaussian window, σ=0.16, μ<sub>n</sub> = mean of the elements that fall in the intervall [μ<sub>n-1</sub>±2σ]
- μ<sub>0</sub> = Starting points



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### **Tracking: Features Distribution**



### Anomaly detection algorithms: PCA

Covariance matrix evaluation

$$\boldsymbol{\Sigma} = \frac{\mathbf{X}^{\mathrm{T}} \mathbf{X}}{N_{\mathrm{X}} - 1}$$

• Eigenvalues decomposition

$$\mathbf{\Sigma} = \mathbf{V} \mathbf{\Lambda} \mathbf{V}^{\mathrm{T}}$$

 Projection in a lower dimensional feature space

$$egin{array}{lll} \mathbf{V}_P &=& [\mathbf{v}_1 | \mathbf{v}_2 | \dots | \mathbf{v}_P] \ \mathbf{X}_P &=& \mathbf{X} \mathbf{V}_P \end{array}$$

Reconstruction

$$\widetilde{\mathbf{X}} = \mathbf{X}_P \mathbf{V}_P^{\mathsf{T}}$$

• Error evaluation (Euclidean distance)

$$e_{x_n} = \sqrt{\sum_{d=1}^{D} (x_{n,d} - \widetilde{x}_{n,d})^2}$$



#### **Confusion Matrix**



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### Anomaly detection algorithms: KPCA

• **Remapping** of the points in a new feature space (**RBF**)

 $K_n^{(\mathbf{z})} = e^{-\gamma ||\mathbf{z} - \mathbf{x}_n||^2}$  with  $n = 1, 2, \dots, N_X$ 

- Application of the PCA algorithm to the new points
- Error evaluation (Euclidean distance)

$$e_{x_n} = \sqrt{\sum_{d=1}^{D} (x_{n,d} - \widetilde{x}_{n,d})^2}$$

where  $D = N_X$   $x_n = K_n$  $\tilde{x}_n = \tilde{K}_n$ 





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### Anomaly detection algorithms: GMM

- Model order selection
  M = 10
- Random initialization of M Gaussian functions with covariance matrix ∑<sub>m</sub> and mean value µ<sub>m</sub>
- Parameter optimization (stochastic gradient descent) to best fit the data distribution
- Threshold setting to ensure a false alarm in the training set equal to 0.01



### Anomaly detection algorithms: ANN



 Mapping in a low dimensional feature space (bottleneck)

 $f_1, f_2 \rightarrow k_1$ 

• **Remapping** in the starting feature space minimizing the reconstruction error

$$k_1 \rightarrow \tilde{f_1}, \tilde{f_2}$$





### Anomaly detection algorithms: OCCNN



Density estimator (Pollard's estimator)

$$\widehat{\lambda}_{\mathbf{X}} = \frac{\left(\sum_{n=1}^{N_{\mathbf{P}}} k_n\right) - 1}{\pi \sum_{n=1}^{N_{\mathbf{P}}} r_n^2}$$

 $\hat{\lambda}_x$ =estimated density,  $N_p$ =n points,  $k_n = k_n$ -th neighbor,

 $r_n$  = distance from the  $k_n$ -th neighbor

- Hyper parameters setting  $\alpha_1 = 0.3, \alpha_2 = 0.8$
- Feed-forward NN with two hidden layers and 50 neurons in each layer

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#### **Confusion Matrix**



### Anomaly detection algorithms: Comparison



#### PREDICTIVE VALUES

Prec+Rec

### Conference papers: Anomaly detection on Z-24

#### One Class Classifier Neural Network for Anomaly Detection in Low Dimensional Feature Spaces

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developed to solve one-class classification (OCC) problems for anomaly detection. Many of them rely on offiniting the statistical distribution of the data, find hidden patterns, or remap the data in advantageous feature spaces. This kind of techniques usually needs some a priori knowledge of the data distribution (i.e., Gaussian) or the setting of some parameters to achieve good classification performance, making their use less effective when the data distribution is unknown. In this paper, we propose a novel blind anomaly detection for low dimensional feature spaces, that exploits the flexibility of the neural network (NN) structure to find the class boundaries without any information about the shape of the data distribution. To prove the generality of the solution, we tested many different class shapes, and we applied it to a structural health monitoring (SHM) case study. Without requiring the tuning of hyperparameters, the performance of the proposed algorithm overcomes that of some known approaches like principal component analysis (PCA), kernel principal component analysis (KPCA), Gaussian mixture model (GMM), and autoassociative neural network (ANN) in many cases, and performs well in the specific SHM setting.

#### I. INTRODUCTION

In the least decade, we have witnessed the rise of cyberphysical systems (CPSs) as the new era of interconnected objects. CPSs consist of sensors to monitor the physical environment and make decisions to affect physical processes through closed-loop controls. These systems will be widely adopted in critical infrastructures, such as oil and natural gas distribution, electrical power grid, industrial automation, the need of hyperparameters. Our solution relies on density automotive, and medical devices [1]-[5]. Therefore, system estimation of the training data distribution, the generation parameter monitoring and behavior classification are becom- of an adversarial class to represent the possible anomalies, ing of paramount importance. Another fascinating application and finally, the training of a NN with the two classes. The domain for CPSs will be structural health monitoring (SHM) same procedure is repeated twice to improve NN detection for the timely detection of damage on a structure, its location, capability. and type with application ranging from historical buildings to large infrastructures.

Abstract-In the last decade, many approaches have been when the normal class boundaries are non-linear, and the data distribution is unknown, a blind solution able to find complex patterns becomes really suggestive.

Nowadays, many different techniques are widely used to solve OCC problems [10]. In this paper, principal component analysis (PCA) [11], [12], kernel principal component analysis (KPCA) [13], Gaussian mixture model (GMM) [10], and autoassociative neural network (ANN) [14], will be presented as a benchmark. These techniques, while effective in some situations, present quite-well known limitations:

- · PCA: finds linear boundaries, so it is recommended only if the data are linearly separable in the feature space;
- · KPCA: overcomes the PCA limitations by managing nonlinear boundaries, but needs the choice of an appropriate kernel function;
- · GMM: finds non-linear boundaries but assumes that the data can be described by a mixture of Gaussian distributions and needs the choice of the most appropriate model order:
- · ANN: finds non-linear boundaries thanks to the non linear activation functions present in the hidden layers but works better when the feature space dimensionality is high.

To overcome such limitations, we propose a neural network (NN)-based solution able to find non-linear boundaries without

Throughout the paper, capital boldface letters denote matrices, lowercase bold letters denote vectors, (·)<sup>T</sup> stands for Depending on the domain of application an anomaly is transposition, ||.|| is the l2-norm of a vector, S stands for the called by alternative terms: alien class, abnormal class, outlier Kronecker product, 1 w is a column vector of all ones and size class, and attacker/intruder class. The target of anomaly detec- N, E{-} is the expectation operator, and V{-} is the variance tion is to discern unusual samples in data by learning a model operator. The rest of the paper is organized as follows. In that accurately describes normality. Generally, this is solved as Section II the data set and data normalisation are described. an unsupervised learning problem where the training dataset. Section III provides an overview of existing OCC techniques. consists of normal samples since the anomalous samples are The one class classifier neural network (OCCNN) is presented not known a priori. This type of problem is also known as in Section IV. Numerical results and a case study are given in one-class classification (OCC) [6]-[9]. From this perspective, Section V and Section VI, respectively. Conclusions are drawn

### FUTURE EXTENSIONS

- High dimensional feature space
- New damage sensitive feature extraction

**\* PCA** \* KPCA \* GMM Stress test Hyperparameter setting Z-24 case of study \* Accuracy Precision \* Recall ✤ F1 score Algorithm comparison ✤ F1 > 93% with OCCNN

\*accepted ICSPCS, Australia, December 2019

- Beacon extraction
- WiFi standard
- Power spectrum density (PSD)
- Beacon average
- \* **PCA**
- **KPCA**
- Received signal strength (**RSS**) based algorithms
- Algorithm comparison
- **☆** Acc > 95% with only 1 beacon (**KPCA**) without signal demodulation

### \*accepted ICSPCS, Australia, December 2019

#### Anomaly Detection Using WiFi Signals of Opportunity

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Abstract-Detection of changes in indoor areas and controlled it gained considerable attention in the last decade. A human environments is getting increasing interest in ambient intelligence and security. In this paper, we propose a radio-frequency (RF)-based anomaly detector that, observing the spectrum received from signals of opportunity (SoOp) and exploiting machine learning (ML) techniques, is capable of revealing changes in an indoor environment. Based on real waveforms emitted by a WiFi susceptible to multipath propagation and need a multitude access point (AP) and collected by a RF sensor, we demonstrate access point (AF) and checked by a broad of the presence of that anomaly detection, e.g., represented by the presence of a person in the monitored area, is possible. The proposed methodology, tested in a typical office environment when the APsensor link is in non-line-of-sight (NLOS), achieves an accuracy greater than 95 % just by collecting few beacon packets, i.e., in dozens of milliseconds. Moreover, results demonstrate that the proposed approach outperforms a well-known received signal rength (RSS)-based solution in terms of accuracy, even using just a single sensor.

#### I. INTRODUCTION

With the advent of the technological revolution named internet of things (IoT), increasingly pervasive and context- SoOp is presented. adaptive communication systems are conquering the radiofrequency (RF) spectrum [1]. Since spectrum population may techniques, either using dedicated sources with large bandrepresent an issue in some frequency bands, e.g., the over- width [16], or using sources of opportunities [17] with crowded industrial, scientific and medical (ISM) ones, there smaller bandwidth but in large environments that ensure taris an increasing interest in exploiting existing over-the-air get/anomaly spatial resolution. However, our goal here is to signals, devised for some specific purpose, to perform other avoid dedicated signals with very large bandwidth and perform tasks thus avoiding dedicated radio emissions. WiFi routers, anomaly detection with SoOp even when the target/anomaly broadcast stations, and mobile cellular networks are only a is not spatially resolvable. few examples of such signals of opportunity (SoOp) [2]-[5].

Security in homes, industrial environments, and facilities is anomaly detection in an indoor environment using WiFi SoOp. becoming a critical aspect of modern society, and for such In particular, the main contributions are the following. reasons, ambient intelligence is gaining attention recently [6]. Video-based surveillance systems using, for example, cameras are the dominant technology in such scenarios. However, the personal privacy issue is still a reason for deterring users. The ambient intelligence paradigm is not only beneficial for security purposes but more generally as an enabler for contextaware applications like smart homes, to name one example.

The capability to extract information from the effects of the propagation on RF signals opens up a way to acquire knowledge about an environment by the observation of SoOp. In this context, there are two main characteristics of the observed signal used for detection, one is the received signal strength (RSS), and the other is channel-state information (CSI). The RSS is very easy to get with simple hardware, so

motion localization method that exploits standard deviation of RSS is presented in [7], [8], and the detection and tracking of multiple persons in an indoor environment is proposed in [9]. However, techniques that exploit received power are of devices to be effective, even when confined in indoor environments [10], [11]. Channel estimation allows greater precision when used in motion detection compared to RSS measurements. In [12], fine-grained subcarrier information (i.e., channel frequency response) is exploited to design a device-free passive human detection. In [13], a scheme for adaptive indoor passive detection is proposed, where the CSI amplitude measured in an indoor environment is shown to vary in the presence of human motion. In [14] the authors propose a device-free RF environmental vision system based both on RSS and CSI, while in [15] a crowd counting system that uses

Target/change detection can also he performed with radar

This work proposes a machine learning (ML) approach for

- · We use inexpensive RF sensors to collect SoOp [18]. Environmental changes are detected through RF channel modifications without demodulating the signal.
- · In particular, we record and analyze samples that belong to beacon packets transmitted by an access point (AP).
- · We compare the performance of two ML classifiers such as principal component analysis (PCA) and kernel principal component analysis (KPCA), as a function of the number of beacon packets collected [19].
- · The tests have been performed in both line-of-sight (LOS) and non-line-of-sight (NLOS) conditions.
- · Finally, we show that the proposed approach exhibits superior performance than a well-known RSS-based solution in terms of accuracy, even using just a single sensor.

### FUTURE EXTENSIONS Target detection trough wall Target localization

### **Conference papers: Topology inference**

#### Machine Learning for Wireless Network Topology Inference

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wireless network topology inference and present a novel solution based on machine learning (ML) techniques. In particular, we seek to identify a causal relationship between the patterns of the radio-frequency (RF) transmissions of the nodes in the network from over-the-air signals observed by a cloud of sensors uniformly distributed in the network landscape. The proposed inferring which nodes are actually communicating, ha framework is based on simple RF sensors that measure the upon the patterns of their activity, might be very useful. received power at a rate sufficient to extract traffic patterns. Numerical results based on simulated data show how, despite the propagation impairments and noise may affect the performance of the algorithms, the neural network (NN)-hased solution reaches 93% of accuracy even with a relatively low number of sensors.

#### I. INTRODUCTION

The importance of networks, in their broad sense, is rapidly and massively growing in modern-day society thanks to unprecedented communication capabilities offered by technology. This aspect is even more exacerbated by the upcoming, A. Existing works if not already happening, revolution of cyber-physical systems (CPSs).

knowledge of network topology, at different levels of abtraffic flow, infer the potential receivers of a currently active making predictions, and designing decision-making strategies.

In many of the above-mentioned scenarios, it seems very important, if not mandatory, that network topology is inferred without the need of being a part of it or without increasing the (AR) model introduced in [10] for econometric time series this reason, in the last decade, there has been an increasing neuroscience and neuroimaging, studying the interactions bea network from few observed quantities at some nodes (or based techniques allow the identification of a threshold on at the edges) with little, if not zero, a priori knowledge of a parametric statistical test to make a decision [13], [14]. the network structure [3], [4]. If the problem appears rather A specific formulation of GC named asymmetric Granger complicated for a wired network, it can be even more chal- causality (AGC) is exploited in [15], where the parametric tests

Abstract-In this work, we propose a new framework for blind large wireless network, on one side, the potential connection between the nodes could be inferred, for example, based upon the distance between them. On the other side, many nodes can be within communication range of many others and have the potential to communicate with all of them. In this situation, inferring which nodes are actually communicating, basing

> Focusing on wireless networks, the rapidly growing demand for radio services by billions of devices will make the radio spectrum an increasingly valuable resource. From this perspective, cognitive radio (CR) devices will have to probe the RF scene in time, space and frequency domain to ensure that a well-defined portion of the spectrum is free, making multidimensional spectrum analysis mandatory [5], [6], [7]. In this context, spectrum awareness, for which network topology plays a crucial role, will be of paramount importance.

There are different approaches and methodologies for network topology inference proposed in the literature. Some of In this scenario of ultra-densely connected objects the them, such as [8], exploit spectral coherence as a measure of causality between two signals. Hence, a decision test with stractions, is an essential aspect that can help to predict a threshold is used to detect causal relations in the traffic generated by the nodes. The main issue of this approach is transmitter, understand the degree of connectivity of users, that it is challenging to choose the correct frequency and the detect the presence of communities, help network mainte- optimal threshold for the decision test. Moreover, solutions nance, optimization, and orchestration. Moreover, in defense of this kind rely upon the notion of correlation which, in applications, understanding the structure of an adversary's principle, does not necessarily imply causation. The task of network may considerably help to avoid dangerous situations, network topology inference can be seen as learning temporal causal structures among multiple time series. This reminds the well-known causality inference problem described by Pearl [9] and Granger [10]. In particular, Granger auto-regressive network overhead sharing topology information [1], [2]. For analysis has been employed more recently in computational interest in the possibility of reconstructing the structure of tween neurons in the brain [11], [12]. Granger causality (GC) lenging in a wireless scenario because of channel impairments, are carried out over groups of time series as will be explained interference, path loss, shadowing and fading, and the so- in Section III. Another approach for causal inference on called hidden terminal problem. In fact, if we consider a networks, that is optimum under certain restrictive Markovian

### FUTURE EXTENSION Node localization Blind source separation

### Network simulation

- Spatial filtering
- Excision filtering
- Wifi protocol
- Feature extraction
- Sample mean
- Sample variance
- Channel model
- Granger causality
- Transfer entropy
- \* NN
- Accuracy
- NN provide better performance with lower complexity

\*accepted ICSPCS, Australia, December 2019

### Future works...







### QUESTION

Why OCCNN overcome always the performance of the others algorithms except in the SHM scenario? ANSWER

This happens because the points are **not uniformally distributed** in the feature space hence the **Pollard's** estimator **wrong estimate** density **POSSIBLE SOLUTION** 

Adopt different techniques to estimate non-uniform density NEW SCENARIOS

- Investigate the effects of quantization on the accelerometers data
- Study the effects of sensor failure on the detection accuracy
- Proposal of new technique to extract damage sensitive features Elia Favarelli

## Thanks for the attention!